

# Efficient Simulation for Silicon-on-Insulator Waveguide Electro-Optic Devices

DeGui Sun and Trevor J. Hall  
 Centre for Research in Photonics  
 University of Ottawa, Ottawa, Canada  
 dsun@site.uottawa.ca

Rob Vandusen and T. Garry Tarr  
 Department of Electronics  
 Carleton University, Ottawa, Canada

**Abstract**—This paper simulates the modulation efficiency and response time of free-carrier dispersion (FCD) effect on silicon-on-insulator (SOI) waveguide electro-optic (EO) devices using professional software called MEDICI. The dependence of free-carrier concentration on the applied voltage and device parameters and the corresponding response time are obtained, typically supporting a  $\sim 10^{19} \text{cm}^{-3}$  concentration variation and a 10-30ns response time at 1.5-2.0V voltage.

**Keywords:** SOI waveguide; FCD; doping density; modulation efficiency of free carriers; response time of modulation process

## I. INTRODUCTION

Demand for next-generation optical networks capable of high-capacity, high-speed and high-agility has been driving the research and development of new components and systems with highly integrated technologies [1], and as such silicon photonic integrated circuit (PIC) technology shows its exclusive merit in applications [2].

In silicon PIC systems, the essential technology for implementing high-speed active parts is a big challenge and a typical illustration is the electro-optic (EO) modulation of silicon-on-insulator (SOI) waveguide devices. The free-carrier dispersion (FCD) effect of the single-crystalline silicon material has been attracting research, but it also induces an extra optical absorption, leading to optical loss at the EO interaction area and intrinsic limitations in device performance [3,4]. The wide acceptability of SOI-PIC technology for the next-generation optical networks is also owing to its compatibility with the micro-electronic infrastructure [2].

## II. ANALYSIS FOR FCD BASED EO MODULATION

### A. Analysis for the FCD-based EO modulation

Unlike the traditional EO modulation of the LiNbO3 waveguide in which the refractive index of waveguide channel is modulated by an effective electric field, in the FCD based EO modulation the refractive index modulation is implemented by a concentration variation of free carriers in the waveguide followed by a negative effect - optical extra-absorption [2-4], which are defined at  $\lambda=1550\text{nm}$

$$\Delta n = -[8.8 \times 10^{-22} \Delta N_e + 8.5 \times 10^{-18} (\Delta N_h)^{0.8}] \quad (1)$$

$$\Delta \alpha = 8.5 \times 10^{-18} \Delta N_e + 6.0 \times 10^{-18} \Delta N_h \quad (2)$$

Where  $\Delta n$  and  $\Delta \alpha$  are respectively the changes of refractive index and absorption coefficient resulting from the concentration variations of free electrons and holes ( $\Delta N_e$  and  $\Delta N_h$ ), respectively. As discussed below, apart from the electric field created in the waveguide,  $\Delta N_e$  and  $\Delta N_h$  are also dependent on some other parameters of devices such as the terminal structure, the background and contact doping densities of free carriers.

### B. Device structure for EO modulation

As shown in Fig. 1, an electrical field is applied to a typical SOI rib waveguide by using a bi-terminal scheme of electrodes: the source and drain terminals.

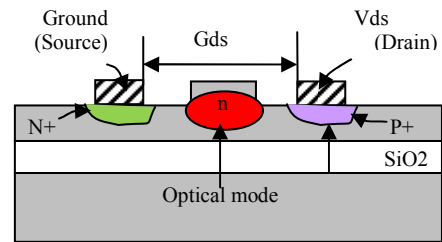


Figure 1. Cross-sectional view of FCD modulation scheme for SOI-waveguide

## III. SIMULATION FOR MODULATION PROCESS

The outside applied voltage  $V_{ds}$  produces a new electric field distribution along x-direction  $E_x$  in EO modulation system shown in Fig. 1, and further forms a drive force to the free carriers (holes) transporting from the drain terminal. This transporting process forms two parts of free-carriers – holes: the original holes  $p$  and the generated excess holes  $\delta p$  [5]. For  $p$ , we have

$$E_x \approx (V_{ds} / G_{ds}) \cdot \gamma \approx e \mu_p P / \sigma \quad (3)$$

$$p \approx (\sigma / e \mu_p) \cdot (V_{ds} / G_{ds}) \cdot \gamma \quad (4)$$

$\gamma$  is an attenuation factor of electric field along y-direction and less than 1.0 and  $\mu_p$  is the mobility of free holes of silicon material. But, for  $\delta p$ , we have

This work is sponsored by National Science & Engineering Research Council (NSERC) with the Program of Idea-to-Innovation (i2i) Phase-I and D&T Photonics.

$$\delta p(x, t) \approx \frac{e^{-t/\tau_{p0}}}{(4\pi D_p t)^{1/2}} \exp\left[\frac{-(x - \mu_p E_x t)^2}{4D_p t}\right] \quad (5)$$

Where  $D_p$  and  $\tau_{p0}$  are the diffusion coefficient and the excess minority free-carrier hole lifetime. Notice from (4) and (5) that the increase of free carriers is a function of time and the above parameters. The total concentration of holes should be  $p_t = p + \delta p$ . Because  $E_x$ ,  $\gamma$  and  $\sigma$  are the complicated functions of several parameters such as  $V_{ds}$ ,  $G_{ds}$ ,  $N^+$  and  $P^+$ , the more accurate solution to the total concentration increase of free holes  $p_t$  should be simulated with a powerful software tool.

#### A. Simulation for the concentration of free carriers

For the device structure shown in Fig. 1, with a professional software tool – MEDICI, we simulate the relationship between  $\Delta N_h$  and  $V_{ds}$  with respect to different gap values. In our simulations, two points should be noted: (i) in terms of basic physical principles of semiconductor devices in transport process of free carriers, the increase of free carriers with applied voltage  $V_{ds}$  should be the same for electrons and holes, which has also been validated by our simulation results and (ii) in terms of (1)  $\Delta N_h$  is extremely dominant to contribute the refractive index modulation compared to  $\Delta N_e$ . Thus, we only need to consider the increase of free holes in the applications of FCD-based EO modulation. For two gap values: 5 and 10 $\mu\text{m}$ , and two sets of the background doping and the contact doping densities underneath the two electrodes as DOPS1:  $n = 1.0 \times 10^{15} / \text{cm}^3$  &  $N^+(P^+) = 1.0 \times 10^{19} / \text{cm}^3$ ; and DOPS2:  $n = 1.0 \times 10^{18} / \text{cm}^3$  &  $N^+(P^+) = 3.0 \times 10^{21} / \text{cm}^3$ , we obtain the relationship between  $\Delta N_h$  and  $V_{ds}$  in the guided-mode as shown in Fig. 2.

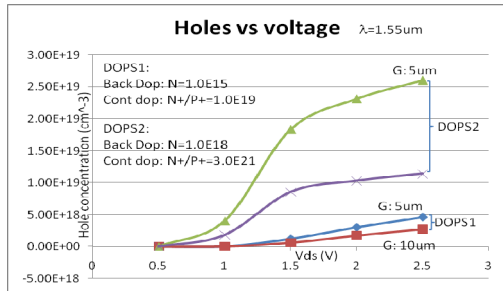


Figure 2. MEDICI simulation results of concentration of free carriers (holes) vs. drive voltage  $V_{ds}$  in the SOI-waveguide mode with respect to gap

Note that the general trend is a higher doping set produces higher  $\Delta N_h$  under the same  $V_{ds}$  and  $G_{ds}$  values. For the low doping set (DOPS1), only when  $V_{ds}$  is greater than 1.0V, the free carrier concentration can start to increase and is strongly dependent on the gap between two terminals; but for the high doping set (DOPS2),  $\Delta N_h$  quickly increases with  $V_{ds}$  and sensitively depends on  $G_{ds}$ .

#### B. Simulation for transport time of free carriers

In terms of the physical principle of semiconductor devices, the transport time of free carriers are also determined by several parameters of device structure and it directly determines the response speed of this modulation process. By taking the same values of parameters as for simulating the concentration of free carriers, we obtain the simulation results of the relationship between the concentration increase of free carriers and the response time in this process as shown in Fig. 3.

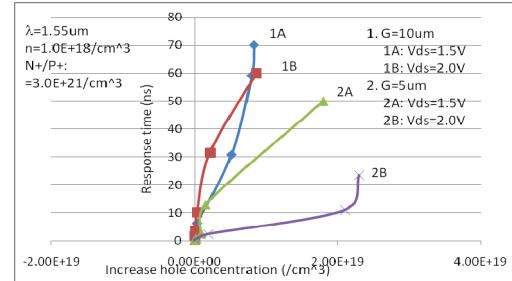


Figure 3. MEDICI simulation results of concentration of free carriers (holes) vs. response time in the SOI-waveguide mode with respect to gap and voltage

Note that both  $G_{ds}$  and  $V_{ds}$  value can have significant influences upon the response time of the modulation process of free carriers. For instance, the case of small  $G_{ds}$  (5um) only needs 10-30ns to reach a hole increase of  $\sim 1.0 \times 10^{19} / \text{cm}^3$ , but the case of big  $G_{ds}$  (10um) needs  $\sim 60$ ns to reach a hole increase of  $\sim 5.0 \times 10^{18} / \text{cm}^3$ .

#### IV. CONCLUSION

The efficient simulations for the concentration distribution of free carriers and response time in the FCD-based EO modulation show the performance of the SOI-waveguide EO devices with the FCD effect can be effectively optimized with this regime and reliable data obtained in simulations.

#### ACKNOWLEDGMENT

Authors thank Z. Hu, S. Abdul-Majid, I. Hasan, Q. Zheng, and A. Hassien for their cooperation. Authors also thank Mr. Peng Liu of D&T Photonics for his support to this work.

#### REFERENCES

- [1] ‘Photonics Integration & Future of Optical Networking’, Heavy Reading Report Vol. 6, No. 3, March 2008.
- [2] Silicon Photonics: The State of the Art, G. T. Reed Eds., John Wiley & Sons: New Delhi, India, 2009.
- [3] R. A. Soref and J. P., Lorenzo “All silicon active and passive guided-wave components for  $\lambda = 1.3\mu\text{m}$  and  $1.6\mu\text{m}$ ,” *IEEE J. Quantum Electron*, vol. QE-22, pp.873-879, 1986.
- [4] D. G. Sun, S. A. Majid, Z. Hu, R. Vandusen, I. Hasan, T. G. Tarr, and T. J. Hall, “An intrinsic limitation to silicon-on-insulator waveguide Mach-Zehnder interference based electro-optic devices,” *Proc. of SPIE*, vol. 7847, Paper-78470P, Beijing, China, Oct 2010.
- [5] D. Eamen, An Introduction to Semiconductor Devices, D. Eamen Eds., John Wiley & Sons: New Delhi, India, Chaps. 4 and 8, 2009.